Introduction to Gravitational Wave Physics



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http://www.oit.ac.jp/is/shinkai/



Einstein-Gauss-Bonnet gravity spherically symmetric spacetimes black hole formation massless scalar field anti-de Sitter space Gauss-Bonnet gravity Klein-Gordon expansion of the universe gravitational collapse positive cosmological constant extrinsic curvature gravitational collapse positive cosmological constant extrinsic curvature de Sitter Conformal factor cosmic censorship Schwarzschild black hole LIGO-Virgo Newtonian scalar-tensor gravity naked singularity gravitational inflationary models gravitational waves Kerr black hole conjecture Planck mass Gauss-Bonnet term plane symmetric evolution equations horizon theory of gravity bubble tensor modes binary neutron star spacetime space-time general relativity neutron star binary flat spacetime eigenvalues hair flat spacetime eigenvalues hair five-dimensional Maxwell testbed Lorentzian inflation LIGO diagonalizable Weyl tensor nical variables ghost Brans-Dicke vacuum spacetimes Gauss-Bonnet general relativistic inflaton field global monopole equation wormhole boson stars gravity general relativistic field equations dynamical variables ghost Brans-Dicke Reissner-Nordstrom throat Constraint propagation scalar field 90% confidence level linear perturbations asymptotic black hole hyperbolic Brans-Dicke theory scalar modes training braneworld black hole hyperbolic Brans-Dicke theory scalar modes that the second scalar modes t constraint equations Hamiltonian constraint four-dimensional post-Newtonian apparent horizon gravitational radiation rotating black holes de Sitter spacetime gravitational wave signals cosmological constant gauge conditions Schwarzschild spacetime radiation reaction higher dimensional spacelike hypersurfaces inflationary scenario spherically symmetric gravitational waveforms inflationary universe numerical integration dynamical equations gravitational-wave bursts search for gravitational waves Recently used

https://scimeter.org says.

2コマ目は, 「Intro to Gravitational Data Analysis」

2020-2-20 山口大学セミナー

1. Gravitational Waves

First Detection (2015 Sep 14)

2017 Novel Prize



2016年2月, LIGOが重力波を初めて検出した, と発表 GW150914



Rainer Weiss Barry C. Barish Kip S. Thorne

"for decisive contributions to the LIGO detector and the observation of gravitational waves"

Nobelprize.org

2017年10月、ノーベル財団が、重力波検出 に貢献した3名をノーベル物理学賞として顕彰

2017年10月, LIGO/Virgo 中性子星連星合体観測を発表 GW170817 Gravitational Wave (radiation & propagation) 重力波の発生と伝播

Binary Blackholes, Binary Neutron Stars ブラックホール連星や 中性子星連星





レーザー干渉計

LIGO = Laser Interferometer Gravitational-Wave Observatory Gravitational Wave (radiation & propagation) 重力波の発生と伝播

Binary Blackholes, Binary Neutron Stars ブラックホール連星や 中性子星連星



ノーザー干渉計

IGO = Laser Interferometer Gravitational-Wave Observatory



重力 = 時空のゆがみ gravitation = space-time warp

質点が加速度運動 = 重力波発生 accelerate motion = GW production

大質量の天体が激しく加速度運動 = 観測できる重力波が発生 Large-mass astrophysical accel. = observable GW



<u>www.phdcomics.com</u> "gravitational waves explained"

重力波の波源 (GW sources)

http://gwcenter.icrr.u-tokyo.ac.jp



What we can learn from GW? (重力波観測によって解明できること)



Test of GR at strong gravity region. 一般相対性理論は正しいか? 強い重力場で重力理論の検証ができる



Test of BH no-hair theory ブ**ラックホール合体後のふるまいは?** no hair になるか. (質量,角運動量,電荷の3物理量のみか?)



Sources of Gamma-ray bursts ガンマ線バースト現象の起源は? 加速メカニズムは?

What we can learn from GW? (重力波観測によって解明できること)



Mechanism of Supernovae 超新星爆発のメカニズムは?

ブラックホールと中性子星の質量差?



Equation of State of nuclear matter 中性子星の最大質量は?

高密度物質の状態方程式は?



Origin of heavy elements

重元素の起源? r-processは充分に発生するか?

Neutron Star Mass-Radius diagram: Equation of State



Figure created by Norbert Wex. EOSs tabulated in Lattimer & Prakash (2001) and provided by the authors.

Hisaaki Shinkai (真貝 寿明) 2020/2/20 @ Yamaguchi Univ.

What we can learn from GW? (重力波観測によって解明できること)



Origin of Supermassive Blackholes 銀河中心の超巨大ブラックホールの起源は? 合体成長か,初期にできていたか?



Cosmological Parameters 宇宙の膨張速度の測定 Stellar formation scenario 星形成モデルの特定 Early Universe before CMB CMB以前の初期宇宙の解明

What we can learn from GW? (重力波観測によって解明できること)



Introduction to Gravitational Wave Physics 1. Gravitational Waves

What can we learn from gravitational waveform?



Discoveries end in an illusion (1968/70)



Joseph Weber

Joseph Weber (**pictured**), a physicist at the University of Maryland in College Park, believed that gravitational waves were real. In 1969, he announced that he had found them with a detector of his own invention: an aluminium cylinder, about 2 metres long and 1 metre in diameter, that 'rang' when it was struck by such a wave². His result was never replicated, and was eventually rejected by nearly everyone except Weber himself. Nonetheless, his work drew many other researchers into the gravitational wave field.

68年に「2台の装置で同時に重力波信号を検出」

70年に「重力波信号はおよそ一日に三回の頻度で 検出され、検出装置が銀河の中心に対して垂直方向 に向いているときに検出率が高い」

と発表したが,他のグループで追試されず.



重力波の存在は連星パルサーの発見で, 間接的に確かめられていた. 重力波の直接観測をしたい!

Binary Blackhole Binary Neutron Stars

Inspiral

Merger Ringdown





Discovery of Binary Neutron Stars (1974)



Pulsar = **Neutron Star** radius 10 km mass 1.4 Msun



Arecibo, Puerto Rico



http://www.nobelprize.org/nobel_prizes/physics/laureates/1993/illpres/discovery.html

Discovery of Binary Neutron Stars (1974)







Period reduction by losing energy by GW. 重力波を放出してエネルギーを失うので, 星が近 づいてゆく.

∃ Grav. Wave, indirect proof

Discovery of Binary Neutron Stars (1974)



"for the discovery of a new type of pulsar, a discovery that has opened up new possibilities for the study of gravitation"

"重力についての新しい研究を開いた,新 種のパルサーの発見に対して" Period reduction by losing energy by GW. 重力波を放出してエネルギーを失うので, 星が近 づいてゆく.

∃ Grav. Wave, indirect proof

Grand Challenge for Black hole simulation (1990s)





2つのブラックホールの合体と重力波放出 (90年代, NCSAグループ)

Simulation of a Binary BH merger



NCSA-AEI group (1998)

3. Detectors LIGO, Virgo, KAGRA



Introduction to Gravitational Wave Physics

KAGRA (かぐら:大型低温重力波望遠鏡)



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レーザー干渉計による重力波検出のしくみ



https://imgur.com/gallery/0VhrXPV

重力波レーザー干渉計に対する工夫 (1)

干渉計は、大きければ大きいほどよい



重力波レーザー干渉計に対する工夫 (2)

さらに、信号を増幅させる



重力波レーザー干渉計に対する工夫 (3)

さらに、さらに、雑音を減らす



KAGRAでの 雑音対策

①地面振動

- ・地下に検出器を設置する
- ミラーを大きな振り子に吊るす





KAGRAでの 雑音対策



180Wのハイパワーレーザーを使う



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LIGO: The Laser Interferometer Gravitational-Wave Observatory

Alex Abramovici, William E. Althouse, Ronald W. P. Drever, Yekta Gürsel, Seiji Kawamura, Frederick J. Raab, David Shoemaker, Lisa Sievers, Robert E. Spero, Kip S. Thorne, Rochus E. Vogt, Rainer Weiss, Stanley E. Whitcomb, Michael E. Zucker

The goal of the Laser Interferometer Gravitational-Wave Observatory (LIGO) Project is to detect and study astrophysical gravitational waves and use data from them for research in physics and astronomy. LIGO will support studies concerning the nature and nonlinear dynamics of gravity, the structures of black holes, and the equation of state of nuclear matter. It will also measure the masses, birth rates, collisions, and distributions of black holes and neutron stars in the universe and probe the cores of supernovae and the very early universe. The technology for LIGO has been developed during the past 20 years. Construction will begin in 1992, and under the present schedule, LIGO's gravitational-wave searches will begin in 1998.

Einstein's general relativity theory describes gravity as due to a curvature of space-time (1). When the curvature is weak, it produces the familiar Newtonian gravity that governs the solar system. When

The authors are the members of the LIGO Science Steering Group. A. Abramovici, W. E. Althouse (Chief Engineer), R. W. P. Drever, S. Kawamura, F. J. Raab, L. Sievers, R. E. Spero, K. S. Thorne, R. E. Vogt (Director), S. E. Whitcomb (Deputy Director), and M. E. Zucker are with the California Institute of Technology, Pasadena, CA 91125. Y. Gürsel is at the Jet Propulsion Laboratory, Pasadena, CA 91109. D. Shoemaker and R. Weiss are at the Massachusetts Institute of Technology, Cambridge, MA 02129.

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the curvature is strong, however, it should behave in a radically different, highly nonlinear way. According to general relativity, the nonlinearity creates black holes (curvature produces curvature without the aid of any matter), governs their structure, and holds them together against disruption (2). Inside a black hole, the curvature should nonlinearly amplify itself to produce a space-time singularity (2), and near some singularities the nonlinearity should force the curvature to evolve chaotically (3). When an object's curvature varies rapidly (for example, because of pulsations, colli-

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baseline KAGRA 構成図



bKAGRA original configuration

160222_SAITO

3. Detectors

aLIGO, aVirgo & KAGRA : Target Sensitivity





FIG. 3. Simplified diagram of an Advanced LIGO detector (not to scale). A gravitational wave propagating orthogonally to the detector plane and linearly polarized parallel to the 4-km optical cavities will have the effect of lengthening one 4-km arm and shortening the other during one half-cycle of the wave; these length changes are reversed during the other half-cycle. The output photodetector records these differential cavity length variations. While a detector's directional response is maximal for this case, it is still significant for most other angles of incidence or polarizations (gravitational waves propagate freely through the Earth). *Inset (a):* Location and orientation of the LIGO detectors at Hanford, WA (H1) and Livingston, LA (L1). *Inset (b):* The instrument noise for each detector near the time of the signal detection; this is an amplitude spectral density, expressed in terms of equivalent gravitational-wave strain amplitude. The sensitivity is limited by photon shot noise at frequencies above 150 Hz, and by a superposition of other noise sources at lower frequencies [47]. Narrow-band features include calibration lines (33–38, 330, and 1080 Hz), vibrational modes of suspension fibers (500 Hz and harmonics), and 60 Hz electric power grid harmonics.

重力波初検出を発表するDavid Reitze LIGO所長 2016年2月11日



"We had detected gravitational waves. We did it."

"我々は,重力波を検出した.やり遂げたのだ."

https://www.youtube.com/watch?v=aEPIwEJmZyE

Observation of Gravitational Waves from a Binary Black Hole Merger

B. P. Abbott et al.*

(LIGO Scientific Collaboration and Virgo Collaboration) (Received 21 January 2016; published 11 February 2016)

On September 14, 2015 at 09:50:45 UTC the two detectors of the Laser Interferometer Gravitational-Wave Observatory simultaneously observed a transient gravitational-wave signal. The signal sweeps upwards in frequency from 35 to 250 Hz with a peak gravitational-wave strain of 1.0×10^{-21} . It matches the waveform predicted by general relativity for the inspiral and merger of a pair of black holes and the ringdown of the resulting single black hole. The signal was observed with a matched-filter signal-to-noise ratio of 24 and a false alarm rate estimated to be less than 1 event per 203 000 years, equivalent to a significance greater than 5.1σ . The source lies at a luminosity distance of 410^{+160}_{-180} Mpc corresponding to a redshift $z = 0.09^{+0.03}_{-0.04}$. In the source frame, the initial black hole masses are $36^{+5}_{-4}M_{\odot}$ and $29^{+4}_{-4}M_{\odot}$, and the final black hole mass is $62^{+4}_{-4}M_{\odot}$, with $3.0^{+0.5}_{-0.5}M_{\odot}c^2$ radiated in gravitational waves. All uncertainties define 90% credible intervals. These observations demonstrate the existence of binary stellar-mass black hole systems. This is the first direct detection of gravitational waves and the first observation of a binary black hole merger.

DOI: 10.1103/PhysRevLett.116.061102



FIG. 1. The gravitational-wave event GW150914 observed by the LIGO Hanford (H1, left column panels) and Livingston (L1, right column panels) detectors. Times are shown relative to September 14, 2015 at 09:50:45 UTC. For visualization, all time series are filtered

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GW150914





Blackhole merger of 36 Msun + 29 Msun --> 62 Msun.

Lost 3 Msun $E = mc^2$

13億光年先(440 Mpc)
重力波波形を音にすると...



始め2回は実周波数,後の2回は聞えやすいように+400Hz

https://mediaassets.caltech.edu/gwave



Animation of the inspiral and collision of two black holes consistent with the masses and spins of GW170104. The top part of the movie shows the black hole horizons (surfaces of "no return"). The initial two black holes orbit each other, until they merge and form one larger remnant black hole. The shown black holes are spinning, and angular momentum is exchanged among the two black holes and with the orbit. This results in a quite dramatic change in the orientation of the orbital plane, clearly visible in the movie. Furthermore, the spin-axes of the black holes change, as visible through the colored patch on each black hole horizon, which indicates the north pole.

The lower part of the movie shows the two distinct gravitational waves (called 'polarizations') that the merger is emitting into the direction of the camera. The modulations of the polarizations depend sensitively on the orientation of the orbital plane, and thus encode information about the orientation of the orbital plane and its change during the inspiral. Presently, LIGO can only measure one of the polarizations and therefore obtains only limited information about the orientation of the advent of additional gravitational wave detectors in Italy, Japan and India.

Finally, the slowed-down replay of the merger at the end of the movie makes it possible to observe the distortion of the newly formed remnant black hole, which decays quickly. Furthermore, the remnant black hole is "kicked" by the emitted gravitational waves, and moves upward. (Credit: A. Babul/H. Pfeiffer/CITA/SXS.) - See more at: <u>http://ligo.org/detections/GW170104.php#sthash.NZPaW2LT.dpuf</u>

http://ligo.org/detections/GW170104.php

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APPENDIX B: SIMULATION RANKINGS

In this appendix, we enumerate the simulations used in this work, ordered by one measure of their similarity with the data $(\ln L, \text{ in Table III})$. For nonprecessing binaries, Fig. 6 provides a visual illustration of some trends in $\ln L$ versus mass ratio and the two component spins.

TABLE III. Peak Marginalized ln L I: Consistency between simulations: Peak value of the marginalized log likelihood ln L [Eq. (7)] evaluated using a lower frequency $f_{low} = 30$ Hz and all modes with $l \le 2$; the simulation key, described in Table II [an asterisk (*) denotes a new simulation motivated by GW150914, and a (+) denotes one of the simulations reported in LVC-detect [1]]; the *initial* spins of the simulation (using – to denote zero, to enhance readability); the initial χ_{eff} ; the total (redshifted) mass of the best fit; and the starting frequency (in Hz) of the best fit. Though omitting information accessible to the longest simulations, this choice of low-frequency cutoff eliminates systematic biases associated with simulation duration, which differs across our archive, as seen by the last column.

ln L	Key	q	$\chi_{1,x}$	X 1,y	X 1,z	X 2,x	X 2,y	X 2,z	$\chi_{ m eff}$	M_z/M_{\odot}	$f_{\rm start}({\rm Hz})$
272.2	SXS:BBH:0310(*)	1.221							0.00	73.0	15.1
272.1	D12 g1.00 a-0.25 0.25 n100(*)	1.0			0.250			-0.250	-0.00	73.2	20.5
272.1	SXS:BBH:0002[S]	1.0							0.00	73.2	10.0
271.8	D11 q0.75 a0.0 0.0 n100(*)	1.333							-0.00	72.1	23.1
271.8	SXS:BBH:0305(*+)	1.221			0.330			-0.440	-0.02	74.2	14.8
271.6	SXS:BBH:0218	1.0			-0.500			0.500	0.00	73.3	10.6
271.6	SXS:BBH:0198	1.202							0.00	73.4	12.7
271.6	SXS:BBH:0307(*)	1.228			0.320	•••		-0.580	-0.08	70.0	17.0
271.6	GT:BBH:476	1.0			-0.200	•••	•••	-0.200	-0.20	67.9	24.3
271.6	S0 D10.04 q1.3333 a0.45 -0.80 n100	1.334			0.450			-0.801	-0.09	71.9	27.9
271.5	D12.00 q0.85 a0.0 0.0 n100(*)	1.176			•••	•••			-0.00	73.0	20.6
271.5	D12.25 q0.82 a-0.44 0.33 n100(*+)	1.22		•••	0.330	•••	•••	-0.440	-0.02	72.9	20.2
271.5	SXS:BBH:0312(*)	1.203	•••	•••	0.390	•••	•••	-0.480	-0.00	73.9	14.8
271.4	SXS:BBH:0127	1.34	0.010	-0.077	-0.017	-0.061	-0.065	-0.179	-0.09	71.5	14.3
271.4	SXS:BBH:0115	1.07	0.019	0.013	-0.204	0.243	-0.067	0.291	0.04	74.1	13.8
271.3	SXS:BBH:0213	1.0	•••	•••	-0.800	•••	•••	0.800	0.00	73.2	11.7
271.3	UD D10.01 q1.00 a0.4 n100	1.0	•••	•••	0.400	•••	•••	-0.400	-0.00	73.4	26.7
271.2	D12 q1.00 a-0.25 0.00 n100(*)	1.0	•••	•••	•••	•••	•••	-0.250	-0.12	69.4	21.8
271.2	SXS:BBH:0222	1.0			-0.300	•••			-0.15	69.1	12.3
271.2	SXS:BBH:0217	1.0			-0.600			0.600	0.00	73.2	11.9

2016年2月、LIGOが重力波を初めて検出した、と発表した



4. Detections

GW150914

GW150914:FACTSHEET

BACKGROUND IMAGES: TIME-FREQUENCY TRACE (TOP) AND TIME-SERIES (BOTTOM) IN THE TWO LIGO DETECTORS; SIMULATION OF BLACK HOLE HORIZONS (MIDDLE-TOP), BEST FIT WAVEFORM (MIDDLE-BOTTOM)

first direct detection of	gravitational waves (GW) and first direct observation				
of a black hole binary					

	observed by		duration from 30 Hz	~ 200 ms		
	source type	black hole (BH) binary	# cycles from 30 Hz	~10		
	source type			~10		
	date	14 Sept 2015	peak GW strain	1 x 10 ⁻²¹ ±0.002 fm 150 Hz, 2000 km		
	time	09:50:45 UTC	peak displacement of			
	likely distance	0.75 to 1.9 Gly	interferometers arms			
		230 to 570 Mpc	frequency/wavelength			
	redshift	0.054 to 0.136	at peak GW strain			
	ienal to noise ratio	24	peak speed of BHs	~ 0.6 c		
S	ignal-to-hoise ratio	24	peak GW luminosity	3.6 x 10 ⁵⁶ erg s ⁻¹		
	false alarm prob.	< 1 in 5 million	radiated GW energy	2.5-3.5 M⊙		
	false alarm rate	< 1 in 200,000 yr	remnant ringdown free	n. ~ 250 Hz		
	Source Mass	ses Mo	remnant damping tim	e ~ 4 ms		
	total mass	60 to 70	rompont sizo area	$180 \text{ km} 3.5 \text{ x} 10^5 \text{ km}^2$		
	primary BH	32 to 41	remnant size, area	Too kin, 5.5 x To kin		
	secondary BH	25 to 33	consistent with	passes all tests		
	remnant BH	58 to 67	·.			
_			graviton mass bound	< 1.2 x 10*** eV		
	mass ratio	0.6 to 1	coalescence rate of	$2 + 100 \text{ Cm} \text{ s}^3 \text{ sm}^1$		
	primary BH spin	< 0.7	binary black holes	2 to 400 Gpc ° yr		
ę	secondary BH spin	< 0.9	online trigger latency	2 min		
	remnant BH spin	0.57 to 0.72	# offline analysis pipelir	~ 5 mm		
	signal arrival time	arrived in L1 7 ms		165 J		
delav		before H1	CPU hours consumed	~ 50 million (=20,000		
	likoly sky position	Southern Hemisphere		PCs run for 100 days)		
		kely sky position Southern Hemisphere		13		
	likely orientation	tace-on/off	# researchers	~1000, 80 institutions		
	resolved to	~600 sq. deg.		in 15 countries		

Detector noise introduces errors in measurement. Parameter ranges correspond to 90% credible bounds. Acronyms: L1=LIGO Livingston, H1=LIGO Hanford; Gly=giga lightyear=9.46 x 10¹² km; Mpc=mega parsec=3.2 million lightyear, Gpc=10³ Mpc, fm=femtometer=10⁻¹⁵ m, M⊙=1 solar mass=2 x 10³⁰ kg 重力波が検出された! 重力波が検出できた! BHが存在した! BH連星が存在した! 相対論が第0近似として正しい! We detected GW ! We could detect GW !

We could detect GW ! BH exists ! BH binary exists ! GR is right as the 0th order !

Signal-to-Noise Ratio (SNR)

Let the true signal h(t), the function of time, is detected as a signal, s(t), which also includes the unknown noise, n(t):

$$s(t) = h(t) + n(t).$$

The standard procedure for the detection is judged by the optimal signal-to-noise ratio (SNR), ρ , which is given by

$$\rho = 2 \left[\int_0^\infty \frac{\tilde{h}(f) \, \tilde{h}^*(f)}{S_n(f)} df \right]^{1/2}$$

where $\tilde{h}(f)$ is the Fourier-transformed quantity of the wave,

$$\tilde{h}(f) = \int_{-\infty}^{\infty} e^{2\pi i f t} h(t) dt,$$

and $S_n(f)$ the (one-sided) power spectral density of strain noise of the detector, as we showed in Fig. 1.







[LIGO'S GRAVITATIONAL-WAVE DETECTIONS]



4. Detections

2017/10/16

GW170817 : First detection of NSNS merger

連星中性子星合体 重力波検出,多くの天文台が同時観測











400 LIGO - Virgo ESO-NT scale) SOAR ESO-VL -ACS 50 -10 -8 -2 400 600 1000 2000 -12 -6 -4 wavelength (nm) $t-t_c$ (s) GW LIGO, Virg γ-ray Fermi, INTEG wift, AGILE, CALET, H.E.S.S., HAWC, Ko X-ray SC. NuSTAR, Chandra, INTEGRA UV Swift, HST Optical PE. TOROS IR REM-ROS2, VISTA NTT, GROND, SOAR, NOT, ESO-VLT, Kanata Tele Radio MA. OVBO. EVN. e-MEBLIN. MeerKAT. Parkes, SBT. Effelsber ATCA, VLA, ASKAP, VLBA, GMBT -100 -50 10⁻² 10-1 00 0 50 $t - t_c$ (s) t-tc (days) VISTA 1M2H Swope DLT40 Chandra i 11.08h h 11.24h YJK_s 10.86h 9d X-ray MASTER DECam J VLA Las Cumbres 11.31h W 11.40h iz 11.57h 16.4d

Figure 2. Timeline of the discovery of GW170817, GRB 170817A, SSS17a/AT 2017gfo, and the follow-up observations are shown by messenger and

of information are shown for each band/messenger. First, the sh Hisaaki Shinkai (真貝 寿明)form2020/2/20 in @ YamaguchinUnive relevant instruments, facilities, or observing teams are collected at Radio

W

FIRST COSMIC EVENT OBSERVED IN GRAVITATIONAL WAVES AND LIGHT

Colliding Neutron Stars Mark New Beginning of Discoveries

Collision creates light across the entire electromagnetic spectrum. Joint observations independently confirm Einstein's General Theory of Relativity, help measure the age of the Universe, and provide clues to the origins of heavy elements like gold and platinum

Gravitational wave lasted over 100 second:

On August 17, 2017, 12:41 UTC, LIGO (US) and Virgo (Europe) detect gravitational waves from the merger of two neutron stars, each around 1.5 times the mass of our Sun. This is the first detection of spacetime ripples from neutron stars. Within two seconds, NASA's Fermi Gamma-ray Space Telescope detects a short gamma-ray burst from a region of the sky overlapping the LIGO/Virgo position. Optical telescope observations pinpoint the origin of this signal to NGC 4993, a galaxy located 130 million light years distant.

周期表 (periodic table)



Pu

プルトニウム

plutonium

239

Am

アメリシウム

americium

243

Cm

キュリウム

curium

247

Bk

バークリウム

berkelium

247

Cf

カリホルニウム

californium

251

Es

インスタイニウム

einsteinium

252

Fm

フェルミウム

fermium

257

Md

メンデレビウム

mendelevium

258

No

ノーベリウム

nobelium

259

Lr

ローレンシウム

lawrencium

262

Np

ネプツニウム

neptunium

237

actinides

Th

トリウム

thorium

232.0

Pa

ロトアクチニウム

protactinium

231.0

U

ウラン

uranium

238.0

Ac

アクチニウム

actinium

227

‡ 5f



核反応 原子核の組み替えによって莫大なエネルギーが放出 Nuclear Reactions





 $4p \rightarrow {}^{4}He + 2e^{+} + 2\nu_{e} + 2\gamma$

核融合

(nuclear fusion)

合体した方が安定 (エネルギー放出) ${}^{235}_{92}\mathrm{U} + {}^{1}_{0}\mathrm{n} \rightarrow {}^{236}_{92}\mathrm{U} \rightarrow {}^{144}_{56}\mathrm{Ba} + {}^{89}_{36}\mathrm{Kr} + 3 {}^{1}_{0}\mathrm{n}$

核分裂 (nuclear fission) 分裂した方が安定 (エネルギー放出)

核融合も核分裂もどちらもおきる理由は何か? Why both nuclear fusion and fission exist?

結合エネルギー (binding energy)



→ → 質量数(大)

核融合も核分裂もどちらもおきる理由は何か? Why both nuclear fusion and fission exist?

結合エネルギー (binding energy)



Feよりも重い元素があるのは何故か?

Why there is heavy elements than Fe?



KAGRA (かぐら:大型低温重力波望遠鏡)



Hisaaki Shinkai (真貝 寿明) 2020/2/20 @ Yamaguchi Univ.

スーパー・カミオカンデ (ニュートリノ観測装置)

Super-Kamiokande http://www-sk.icrr.u-tokyo.ac.jp/sk/





岐阜県・神岡の鉱山跡の空洞に巨大な水槽をつくり, 宇宙から飛来するニュートリノを観測する.



ノーベル物理学賞を受賞

梶田隆章(2015年)





KAGRA (かぐら:大型低温重力波望遠鏡)



Hisaaki Shinkai

Seiji Kawamura Kieran Craig Martynov Denis



KAGRA (かぐら:大型低温重力波望遠鏡)







KAGRA (かぐら:大型低温重力波望遠鏡)



KAGRA SCIENTIFIC CONGRESS: COLLABORATORS' INFORMATION EXCHANGE

KSC Newsletter

Second Issue

1

From Phase 1 to Phase 2

Nine-day operation with wild weather & earthquakes

KAGRA now has the world's tallest vibration isolation systems (13.5 m) which help to reduce seismic noise at low frequencies. The volume of the vacuum system is third largest in the world. Two 23-kg sapphire mirrors have been installed at each end, and one of them was kept for 30 days at cryogenic temperature (18K).

A leakage of the vacuum system was found in April 2018, therefore the Phase-1 experimental activity was delayed for 5 days. Despite the difficulties, the phase-1 operation was a success: it lasted from April 28 to May 6, 2018, and during this period many injection tests were performed.

The interferometer duty cycle during the Phase-1 operation reached 88.6% between April 28 and May 2, while it dropped to 26.8% on May 3 and 4. Finally it slightly improved to 59.8% over the final days (May 5 & 6). The longest lock was over 10 hours. The low duty cycle on May 3 and on the following days was mainly attributed to the high micro-seismic noise caused by a heavy storm, local earthquakes, volcano eruptions in Hawaii, and visits of theorists.

The achieved sensitivity during Phase 1 was still worse than the final sensitivities of TAMA and CLIO, except at the lower frequencies (40 Hz), where KAGRA's sensitivity was better than that of TAMA. KAGRA started Phase 2 from May 7: the final installation work before the real observation run.



2018/08/01

Weather map of May 3, 2018.



Contents of this issue p-2 Directions Steps to the Observation 2019 p-3 Kamioka local Subgroup orientation Kagra River / Science Cafe p-5 Meetings F2F at Osaka City U. KIW5 at Seoul **Poster Award Winners** Group LOGO Next F2F at Toyama p-8 Virgo Visit p-9 We hear that ...



KSC NewsLetter

The premiere issue

Phase-1 operation starts on April 23

First cryogenic interferometer test will start soon.

After two years from the iKAGRA run, we will start phase-1 operation on April 23 to May 6. Due to the tight schedule for our upcoming real observation, system engineering office (SEO) decided to operate phase-1 with one cryogenic mirror (Yarm), and the other at normal temperature. We do not know what will be the outcomes. So it might become a sort of fun. A detail list of tests planned during the run is at page-3.

O3=Ozone.

The above photo, taken in a clean room in the University of Toyama, is our 23kg-Sapphire mirror for X-end, which is now under installation. The installation of the cryo-payload at X-end is almost done and the main beam is coming back to the center now 😀.



1



What is this



We are in a rush for O3 this year. Let's finish looking for O2.



We call for volunteers We welcome your editorial participation to this journal. It will give you a career update definitely.

http://gwwiki.icrr.u-tokyo.ac.jp/JGWwiki/KAGRA

Organization of KSC (KAGRA Scientific Congress)



KAGRA SCIENTIFIC CONGRESS: COLLABORATORS' INFORMATION EXCHANGE

KSC Newsletter

Issue 6

KAGRA joined International GW Network

Signed up LIGO-Virgo-KAGRA MoA for joint observation

On October 4, 2019, KAGRA held a ceremony to mark the completion of the detector. The ceremony was in the site, and after the play of the music of *kagura* (the traditional Shinto-style ritual music) by local children's musical group, Takaaki Kajita, our PI, pushed a button with U Tokyo Executive Vice President Kohei Miyazono to demonstrate the detector in motion. In the evening of the day, the signing ceremony of a memorandum of agreement (MoA) on a research collaboration between KAGRA, LIGO and Virgo were held.

This MoA makes KAGRA an equal partner of LIGO and Virgo, and once KAGRA satisfied the criteria for joining observation then all the scientific achievements will be presented as LIGO-Virgo-KAGRA collaboration. KAGRA is definitely close to the production phase after the ten-year construction and installation period.



(Above) Pose for photos after signing a MoA. (from left) EGO vice president Christian Olivetto, Virgo spokesperson Jo van den Brand, KAGRA principal investigator Takaaki Kajita, LIGO Executive Director David Reitze, KSC board chair Hisaaki Shinkai, and KAGRA vice PI Masatake Ohashi. At ANA Crowne Plaza hotel Toyama, October 4, 2019. [Photo courtesy of Hida City]



2019/10 LVK MoA signed



International GW network (国際重力波観測ネットワーク)















1330 members860 authors101 groups20 countries

465 members 360 authors 96 groups 8 countries

360 members 200 authors 110 groups 14 regions

Observation 3

Current O3 Schedule (LIGO-G1901531)



Rush to 1 Mpc by February 25, 2020



Target

iKAGRA (8.5e-07 Mpc) bKAGRAPhase1 (2.0e-05 Mpc)

O3 target (8-24 Mpc)

10-23

 10^{-24}

 10^{0}

FPMI20190824 (4.0e-04 Mpc)

FPMI20191127 (2.6e-02 Mpc) bKAGRA Design BRSE bKAGRA Design DRSE

 10^{1}

10²

frequency (Hz)

10³

2020/2/13

http://klog.icrr.u-tokyo.ac.jp/osl/?r=12961



GW observatory plans in space

http://gwplotter.com



Gravitational Wave Detectors and Sources

GW observatory plans in space



重力波宇宙干渉計LISA(リサ) ESA予算承認 2017/6/20 Laser Interferometer Space Antenna



2034年に打ち上げ予定 250万kmの腕の長さ 地球の公転軌道のL4 低周波数帯(mHzからHz帯)



重力波宇宙干渉計DECIGO(ディサイゴ)

Deci-hertz Interferometer Gravitational wave Observatory



1000kmの腕の長さ 低周波数帯(deciHzからHz帯)





周波数[Hz]

宇宙空間光格子時計ネットワーク INO

Interplanetary Network of Optical Lattice Clocks



宇宙全体スケールで 巨大ブラックホール連星合体の 重力波が検出できる





伊能忠敬 江戸時代,日本中で 精密な測量をして地図を作成

「数理科学」2018-12

D 28 (2019) 1940002

「科学」2017-12

Int. J. Mod. Phys.

arXiv:1809.10317

BH連星合体から銀河中心SMBHの形成シナリオを決める

★BH連星合体が繰り返されて,SMBHが形成されると考える ★1つの銀河にいくつBH連星合体があるかを数える

★宇宙にいくつ銀河があるかを数える

★LIGOやKAGRAの検出器感度で、1年にいくつ観測できるのか予想する



Figure 5. Number density of BHs per galaxy as a function of BH mass for different total mass of galaxies $M_{\text{galaxy}} = 10^9 M_{\odot}, \dots, 10^{12} M_{\odot}$.



Figure 6. Cumulative distribution function of the number of BH mergers $N_{\text{merger}}(M_{\text{BH}})$ as a function of the redshift z. N_{merger} is expressed with binned one, of which we binned 20 for one order in M_{BH} .

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Gravitational Waves from Merging Intermediate-mass Black Holes. II. Event Rates at Ground-based Detectors

Hisa-aki Shinkai¹, Nobuyuki Kanda², and Toshikazu Ebisuzaki³
BH連星合体から銀河中心SMBHの形成シナリオを決める

- ★BH連星合体が繰り返されて、SMBHが形成されると考える
- ★1つの銀河にいくつBH連星合体があるかを数える
- ★宇宙にいくつ銀河があるかを数える
- ★LIGOやKAGRAの検出器感度で、1年にいくつ観測できるのか予想する



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Gravitational Waves from Merging Intermediate-mass Black Holes. II. Event Rates at Ground-based Detectors

Hisa-aki Shinkai¹, Nobuyuki Kanda², and Toshikazu Ebisuzaki³

Event Rates at bKAGRA/aLIGO

		2	1			
	$R/(Gpc^{-3} yr^{-1})$					
Mass distribution	PyCBC	GstLAL	. Combined			
	Event bas	ed				
GW150914	$3.2^{+8.3}_{-2.7}$	$3.6^{+9.1}_{-3.0}$	$3.4^{+8.8}_{-2.8}$			
LVT151012	$9.2^{+30.3}_{-85}$	$9.2^{+31.4}_{-85}$	$9.1^{+31.0}_{-8.5}$			
GW151226	35^{+92}_{-29}	37^{+94}_{-31}	36_{-30}^{+95}			
All	53_{-40}^{+100}	56_{-42}^{+105}	55_{-41}^{+103}			
	Astrophysi	cal				
Flat in log mass	31_{-21}^{+43}	29_{-21}^{+43}	31^{+42}_{-21}			
Power law (-2.35)	100_{-69}^{+136}	94_{-66}^{+137}	97^{+135}_{-67}			

LIGO group PRX6(2016)041015





Shinkai+ ApJ 835(2017)276

Kinugawa+ MNRAS456(2015)1093



	宇宙線	ガンマ線	X 線	光			電磁波					
				紫外線	可視光線	赤外線	マイクロ波	超短波	短波	中波	長波	超長波
波長[m]	m] 10^{-13} 10^{-10} 10^{-9} 3.8×10^{-7} 7.7×10^{-7} 10^{-4} 1 10 10^{2} 10^{3} 10^{4}											
波長[nm]				è	880 71	0						
振動数[Hz]	11.11	3×10^{18}	$3 \times$	10 ¹⁷		32	$ imes 10^{12}$ 3 $ imes$	$10^{8} 3 \times$	10^{7} 3	$ imes 10^{6}$	3×10^{5} 3	$ imes 10^4$
利用例		医療/食品照射	医療/X線写真	殺菌	光学機器	赤外線写真	携帯電話	テレビ ジオ	短波ラジオ	AMラジオ	電波時計	

